# 285. The Crystal Structure of 1:12-Benzperylene: A Quantitative X-Ray Investigation. 

By J. G. White.


#### Abstract

The crystal and molecular structure of 1:12-benzperylene has been determined by quantitative $X$-ray analysis. There are four molecules in the unit cell, and the structure resembles that of pyrene, but involves a considerably larger tilt of the plane of the molecule to the (010) plane. The accuracy of the analysis is limited by overlapping of adjoining molecules. In the most favourable Fourier projection, 11 of the 22 carbon atoms in the molecule are resolved and the measured bond distances between these atoms vary from 1.38 to 1.43 A . The variations in bond distances in different parts of the molecule are very similar to the corresponding variations noted in the case of coronene and are discussed in terms of the 14 nonexcited valency-bond structures applicable to 1 : 12-benzperylene.


In recent investigations on the aromatic hydrocarbons coronene, pyrene, and 1:2:5:6dibenzanthracene (Robertson and White, J., 1945, 607; 1947, 358, 1001) small variations in carbon-carbon bond lengths in different parts of the molecules have been detected. In coronene and pyrene these variations are in qualitative agreement with calculations of the bond distances from the non-excited valency-bond structures alone. In the case of dibenzanthracene the agreement between the observed bond distances and those calculated on this basis is not quite so satisfactory, although the experimental data for this compound are rather less certain than for the other two. As has been pointed out in connection with coronene (Robertson and White, loc. cit.) the apparent agreements may be fortuitous, for in such complex molecules the excited structures must play a considerable part. Coulson's rigorous molecular orbital calculations on coronene (Nature, 1944, 154, 797), however, are also supported by the $X$-ray measurements. The structure of $1: 12$-benzperylene ( I ), now described, is of interest in that this molecule differs by only two carbon atoms from that of coronene, and the $X$-ray measurements on coronene are the most accurate of those mentioned above. Unfortunately, the crystal structure of benzperylene is much less favourable for $X$-ray analysis than that of coronene. There are four molecules instead of two in the unit cell and in this respect the structure is similar to that of pyrene (Robertson and White, loc. cit.). Because of the overlapping of adjoining molecules only 11 of the 22 crystallographically independent atoms are resolved even in the most favourable Fourier projection, and accurate molecular dimensions are consequently incomplete. Although some interesting variations in carbon-carbon bond distances have been observed, complete and accurate data can be obtained only from a full three-dimensional analysis of the structure, and, as was the case with pyrene and 1:2:5:6-dibenzanthracene, one of the principal objects of the present investigation has been to refine the atomic parameters to the point where such a three-dimensional analysis can be undertaken.

## Description of the Structure.

Crystal Data.-1:12-Benzperylene, $\mathrm{C}_{22} \mathrm{H}_{12} ; M, 276 \cdot 3$; m. p. $273^{\circ}$; $d$, calc. $1 \cdot 338$, found 1.349 ; monoclinic prismatic, $a=11.72 \pm 0.05, b=11.88 \pm 0.05, c=9.89 \pm 0.03$ A., $\beta=$ $98.5^{\circ} \pm 0 \cdot 2^{\circ}$. Absent spectra, ( $h 0 l$ ) when $h$ is odd; ( $0 k 0$ ) when $k$ is odd. Space-group $C_{2 h}^{5}\left(P 2_{1} / a\right)$. Four molecules per unit cell. No molecular symmetry. Volume of the unit cell, 1362 A. ${ }^{3}$. Absorption coefficient for $X$-rays $(\lambda=1.54), \mu=7.01$ per cm . Total number of electrons per unit cell $=F(000)=576$.

The crystals are in the form of prisms, the most prominent faces being (001) and (110). The (010) face was observed in only one crystal specimen.

Analysis of the Structure.-The asymmetric crystal unit consists of one complete molecule, and as a first approximation a regular, planar, hexagonal, model may be assumed in accordance with the usual chemical formula. Now the $b$-axis in benzperylene is appreciably larger than that of pyrene, viz., $9 \cdot 24 \mathrm{~A}$. (Robertson and White, loc. cit.). This suggests that in benzperylene
also there are two molecules accommodated in one $b$-axis translation, but tilted rather more steeply to (010) than in the pyrene or coronene structures.

A tilt of the molecular plane to (010) of about $55^{\circ}$ being assumed, there remain five more degrees of freedom to be fixed, viz., two more orientation angles and the free translations, $x_{p}, y_{p}, z_{p}$, of the molecular centre (taken as the centre of the central benzene ring) along the three crystal axes from the origin. The approximate orientation of the molecule can be readily


Projection along the b axis on the (010) plane. The overlapping molecules are inclined at about $58^{\circ}$ to the projection plane. Each contour line corresponds to one electron per A. ${ }^{2}$, the two-electron line being dotted.
found by an inspection of the $X$-ray reflections from the small-spacing ( $h 0 l$ ) planes $204,10,04$, $800,60 \overline{9}, 80 \overline{4}$, and $80 \overline{5}$. These reflections are all very strong and hence the contributions from most of the atoms must be in phase. By means of a diagram similar to that constructed for coronene (Robertson and White, loc. cit.) it is found that only one orientation of the molecular model can account for the enhancement of all these reflections.

From a general consideration of the axial sets of reflections ( $h 00$ ) and ( $00 l$ ) it would appear that there is only a small $c$-axis translation of the molecular centre involved, but a comparatively large translation along $a$. The asymmetry of the molecule, however, makes it difficult to
distinguish between possible alternative positions for the molecular centre without very detailed calculations.

This work is shortened considerably by a comparison of benzperylene with perylene, $\mathrm{C}_{20} \mathrm{H}_{12}$ (II), on which a parallel investigation is in progress. The cell dimensions and spacegroup of perylene have been recorded by Hertel and Bergk (Z. physikal. Chem.,
 $1936,33,319$ ) and are very closely related to those of benzperylene. Rotation photographs taken about corresponding axes for the two compounds show a remarkable similarity in intensity distribution, and this can only be due to a very close, three-dimensional similarity in structure.

Now, with perylene, the reflection from the large-spacing (201) planes is too weak to be visible, and as this molecule probably contains an inherent centre of symmetry, it appears that the molecular centre lies on a line one-quarter of the way between the (201) planes. In benzperylene, the (201) reflection is recorded, since the two additional carbon atoms make appreciable contributions to this reflection, but we can assume

Fig. l(b).

from the general structural similarity noted above that the molecular centre of benzperylene lies in approximately the same relative position as that of perylene. When this deduction is considered in conjunction with the earlier observations on the structure of benzperylene, it becomes clear that there is only one reasonable position for the molecular centre, the free translation along the $a$ axis $\left(x_{p}\right)$ being approximately 0.9 A . and that along $c 0.45 \mathrm{~A}$.

Calculations of the ( $h 0 l$ ) structure factors on the above basis led to good agreements with the observed values and it was possible to refine the atomic parameters from this stage by double Fourier series methods. Three successive Fourier analyses of the ( $h 0 l$ ) zone were carried out. In the final refinement 128 terms were included in the series, representing all the reflections which could be observed with copper- $K_{a}$ radiation. The results are shown in the contour map of Fig. $1(a)$. Only 11 out of the 22 crystallographically independent atoms are separately resolved, the others being obscured by overlapping effects of adjoining molecules as shown in Fig. 1(b).

By assuming that the molecule is symmetrical about the axis $M$ (Fig. 1b), it is possible to calculate the $x$ and $z$ co-ordinates of three more atoms, $J, K$, and $Q$, but the remaining eight atoms have been assigned " regularised " co-ordinates as described on p. 1406. These positions are in accordance with the appearance of the observed double peaks in Fig. 1(a), but it would not be possible to detect small displacements from these positions.

The $y$ co-ordinates of all the atoms are calculated on the assumptions that the molecule is planar and that $L$ and $M$ are at right angles. These assumptions are confirmed by the satisfactory agreements between the calculated and observed values of the ( $h k 0$ ) structure factors. The free translation along the $b$-axis must lie within fairly narrow limits from packing considerations, and it has been accurately determined by trial calculations using the observed values of the ( $h k 0$ ) structure factors.

A complete picture of the crystal structure can be built up from Figs. 1 and 2. Fig. 2 shows the approximate appearance of the structure when viewed in a direction perpendicular to the $a$-and the $b$-axis.

Orientation, co-ordinates, and dimensions. By assuming a planar molecule with axes $L$ and $M$ [Fig. 1(b)] at right angles, and averaging certain distances as described more fully on p. 1404, it is possible to calculate precisely the orientation of the molecule with regard to the crystal axes. The results are collected in Table I, where $\chi, \psi$, and $\omega$ are the angles which the molecular axes $L$ and $M$ and their perpendicular $N$ make with the crystallographic axes $a, b$, and $c^{\prime}\left(c^{\prime}\right.$ is perpendicular

Fig. 2.


End view of molecules. to $a$ and $b$ ). The tilt of the molecular plane to the ( 010 ) plane (expressed by $\psi_{N}$ ) is $58 \cdot 2^{\circ}$, very close to the value found for naphthalene (Robertson, Proc. Roy. Soc., 1933, $A, 142,674$ ) but considerably greater than that in the other hydrocarbons

Table I.
Orientation of the molecule in the crystal.

| $\chi_{L}=79.7^{\circ}$ | $\cos \chi_{L}=0.1787$ | $\chi_{M}=58.6^{\circ}$ | $\cos \chi_{M}=0.5216$ | $\chi_{N}=147.4^{\circ}$ | $\cos \chi_{N}=0.8345$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\psi_{L}=91.2$ | $\cos \psi_{L}=-0.0216$ | $\psi_{M}=31.8$ | $\cos \psi_{M}=0.8500$ | $\psi_{N}=58 \cdot 2$ | $\cos \psi_{N}=0.5265$ |
| $\omega_{L}=10.3$ | $\cos \omega_{L}=0.9837$ | $\omega_{M}=94.4$ | $\cos \omega_{M}=-0.0761$ | $\omega_{N}=80.7$ | $\cos \omega_{N}=0.1622$ |

mentioned above. The perpendicular distance between two parallel, overlapping molecules is 3.38 A ., not significantly different from the values found for coronene ( 3.41 A .) and graphite (3.40 A.).

The co-ordinates with respect to the crystal axes are collected in Table II. The measured $x$ and $z$ co-ordinates of the 11 atoms separately resolved in the contour map of Fig. 1 are given in the columns headed (b), while the co-ordinates finally adopted are listed under (a).

The molecular dimensions and bond distances can be calculated from the observed crystal co-ordinates by combination with the orientation angles of Table I and the results are shown in Fig. 3. The ringed atoms $A, B, C, D, G, H, I, P, R, S$, and $T$ are those which are separately resolved in Fig. 1 (a), and bond distances between these atoms alone can be measured directly. The three atoms $J, K$, and $Q$, however, can be assigned accurate co-ordinates on the assumption that the molecule is symmetrical about the axis $M$. This assumption can be tested by a comparison of corresponding pairs of bond lengths on either side of $M$. The results are :

$$
\begin{array}{ll}
R D=1.43 \mathrm{~A} . & S G=1.42 \mathrm{~A} . \\
R Q=1.43 \mathrm{~A} . & S T=1.43 \mathrm{~A} . \\
A B=1.43 \mathrm{~A} . & J I=1.39 \mathrm{~A} . \\
B C=1.39 \mathrm{~A} . & H H=1.37 \mathrm{~A} . \\
C D=1.45 \mathrm{~A} . & H G=1.41 \mathrm{A.}
\end{array}
$$

$$
\text { Mean value }=1.42 \mathrm{~A}
$$

$$
, \quad=1.43 \mathrm{~A}
$$

$$
\begin{array}{ll}
", & =1.41 \mathrm{~A} . \\
" & =1.41 \mathrm{~A} .
\end{array}
$$

$$
\because \quad=1.38 \mathrm{~A} .
$$

$$
\begin{aligned}
\because & =1.43 \mathrm{~A} . \\
\because & =1 .
\end{aligned}
$$

Table II.
Co-ordinates with respect to monoclinic crystal axes : centre of symmetry as origin.

| Atom <br> [cf. Fig. 1(b)]. | $\begin{gathered} x, \mathrm{~A} . \\ (a) . \end{gathered}$ | $\begin{gathered} x, \mathrm{~A} . \\ (b) . \end{gathered}$ | $2 \pi x / a$ $(a) .$ | $\begin{gathered} y, \mathrm{~A} . \\ (a) . \end{gathered}$ | $\begin{gathered} 2 \pi y / b \\ (a) . \end{gathered}$ | $\begin{gathered} z, \mathrm{~A} . \\ (a) . \end{gathered}$ | $\begin{gathered} z, \mathrm{~A} . \\ (b) . \end{gathered}$ | $2 \pi z / c$ $(a)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | 1.832 | $1 \cdot 832$ | $56.3{ }^{\circ}$ | -2.085 | $-63.2^{\circ}$ | $3 \cdot 300$ | $3 \cdot 300$ | $120.1^{\circ}$ |
| B | $2 \cdot 682$ | $2 \cdot 699$ | $82 \cdot 3$ | $-1.051$ | -31.8 | $3 \cdot 880$ | $3 \cdot 898$ | $141 \cdot 2$ |
| C | 3.071 | 3.077 | $94 \cdot 3$ | $-0.017$ | $-0.5$ | $3 \cdot 105$ | 3.096 | $113 \cdot 1$ |
| D | $2 \cdot 617$ | $2 \cdot 617$ | $80 \cdot 3$ | 0.034 | 1.0 | 1.684 | $1 \cdot 655$ | $61 \cdot 3$ |
| E | 2.999 | 2 | $92 \cdot 1$ | 1.072 | $32 \cdot 5$ | 0.883 |  | $32 \cdot 2$ |
| F | $2 \cdot 540$ |  | 78.0 | $1 \cdot 102$ | $33 \cdot 4$ | $-0.519$ |  | $-18.9$ |
| G | $1 \cdot 695$ \| | 1.675 | $52 \cdot 1$ | 0.096 | $2 \cdot 9$ | $-1.136$ | -1.164 | - 41.4 |
| H | 1.219 | 1.208 | $37 \cdot 5$ | $0 \cdot 107$ | $3 \cdot 2$ | $-2.553$ | $-2.558$ | $-92 \cdot 9$ |
| I | 0.380 | $0 \cdot 375$ | 11.7 | $-0.897$ | $-27 \cdot 1$ | $-3 \cdot 134$ | $-3 \cdot 122$ | $-114 \cdot 1$ |
|  | $-0.028$ | - | - 0.9 | $-1.961$ | $-59.4$ | $-2.376$ | - | $-86.5$ |
| K | $-0.870$ | - | $-26.7$ | $-2.979$ | $-90.3$ | $-2.963$ | - | $-107.8$ |
| L | $-1.272$ | - | $-39 \cdot 1$ | $-4.036$ | $-122.2$ | $-2.186$ | - | $-79.6$ |
| M | $-0.812$ | - | $-24 \cdot 9$ | $-4.067$ | $-123.2$ | -0.786 | - | $-28.6$ |
| N | $0 \cdot 128$ | - | $4 \cdot 0$ | $-4 \cdot 129$ | $-125.1$ | 2.086 | - | 76.0 |
| O | $0.586$ | - | 18.0 | $-4 \cdot 160$ | $-126.0$ | $3 \cdot 486$ | - | 126.9 |
| P | $1.435$ | 1.435 | $44 \cdot 1$ | $-3.133$ | - 94.9 | 4.075 | $4 \cdot 075$ | $148 \cdot 4$ |
| Q | $1 \cdot 371$ |  | $42 \cdot 1$ | $\begin{array}{r} -2.060 \\ \hline \end{array}$ | $\begin{array}{r} -62.4 \end{array}$ | 1.899 |  | $69 \cdot 1$ |
| R | $1 \cdot 756$ | 1.755 | $53 \cdot 9$ | $-1.000$ | $-30 \cdot 3$ | 1.073 | 1.076 | $39 \cdot 1$ |
| S | 1.294 | 1.295 | $39 \cdot 8$ | $-0.970$ | $-29.4$ | $-0.335$ | $-0.338$ | $-12.2$ |
| T | 0.430 | 0.430 | $13 \cdot 2$ | $-1.996$ | $-60 \cdot 5$ | -0.974 | -0.974 | $-35 \cdot 4$ |
| U | $0 \cdot 038$ | - | $1 \cdot 2$ | $-3.045$ | $-92 \cdot 3$ | $-0.178$ | - | - 6.5 |
| V | 0.520 | - | 16.0 | $-3.075$ | $-93.2$ | 1.292 | - | $47 \cdot 0$ |
| Molecular centre | 0.907 | 0.907 | $27 \cdot 9$ | $-2.015$ | - 61.0 | $0 \cdot 462$ | $0 \cdot 462$ | 16.8 |

The deviations from the mean values are nowhere greater than $\pm 0.02 \mathrm{~A}$. and these differences are probably due to experimental error. The mean values have been employed in Fig. 3, and the corresponding crystal co-ordinates adopted in Table II under (a).

Fig. 3.


Dimensions of the benzperylene molecule.

Fig. 4.


Normal projection of two parallel molecules.

The bond distances shown in Fig. 3 vary over a range of 0.05 A . In this compound, however, the tilt of the molecule to the projection plane is considerably steeper than in any of the structures previously discussed, with consequent greater uncertainty in the $y$ co-ordinates, and errors in bond length estimates may amount to $\pm 0.03 \mathrm{~A}$. Nevertheless, it seems probable that the more extreme variations noted above, e.g., between $B C$ and $H I$, on the one hand, and the bonds $Q R, R S$, and $S T$ in the central ring, on the other, are real. The smaller variations, however, may be spurious.

The molecular structure is summarised in Table III, where the co-ordinates with respect to the molecular axes $L, M$, and $N$ are listed. These co-ordinates can be combined with the
crystal co-ordinates of the molecular centre and the orientation angles of Table I according to the relations :

$$
\begin{array}{ll}
x^{\prime}=L \cos \chi_{L}+M \cos \chi_{M}+N \cos \chi_{N}+x_{P^{\prime}} & x=x^{\prime}-z^{\prime} \cot \beta \\
y & =L \cos \psi_{L}+M \cos \psi_{M}+N \cos \psi_{N}+y_{P}, \\
z^{\prime}=L \cos \omega_{L}+M \cos \omega_{M I}+N \cos \omega_{N}+z_{P^{\prime}} & z=z^{\prime} \operatorname{cosec} \beta
\end{array}
$$

to give the final crystal co-ordinates of Table II.
Table III.
Co-ordinates with respect to molecular axes.

| Atoms. | $L$, A. | $M$, A. | $N$, A. | Atoms. $L$, A. | $M$, A. | $N$, A. | Atoms. | $L$, A. | $M, \mathrm{~A}$. | $N, \mathrm{~A}$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $A, J$ | $\pm 2.857$ | -0.009 | 0 | $E, F$ | $\pm 0.705$ | 3.650 | 0 | $U, V$ | $\pm 0.740$ | -1.230 | 0 |
| $B, I$ | $\pm 3.535$ | 1.225 | 0 | $K, P$ | $\pm 3.542$ | -1.225 | 0 | $Q, T$ | $\pm 1.445$ | -0.014 | 0 |
| $C, H$ | $\pm 2.847$ | 2.424 | 0 | $L, O$ | $\pm 2.855$ | -2.450 | 0 | $R, S$ | $\pm 0.712$ | 1.211 | 0 |
| $D, G$ | $\pm 1.419$ | 2.447 | 0 | $M, N$ | $\pm 1.445$ | -2.450 | 0 |  |  |  |  |

Intermolecular distances. The closest approach of adjacent molecules occurs along the $b$-axis where there is a perpendicular distance of 3.38 A . between the two molecules related by the centre of symmetry at the origin. Fig. 4 shows the normal projection of one of these molecules in the plane of the other. This diagram is very like the corresponding projection for coronene (Robertson and White, loc. cit.), with a similar staggered arrangement of the atoms of the two molecules. The closest approach in this direction between atoms of different molecules is from $S$ on the standard molecule to $S^{\prime}$, the corresponding atom on the inverted molecule, where the distance is 3.38 A . The three pairs of atoms $D J^{\prime}, F U^{\prime}$, and $Q H^{\prime}$ are 3.39 A . apart.

In other directions the distances are greater. Along the $a$-axis, from $D$ on the standard molecule to $O$, the molecule at $x-\frac{1}{2},-y-\frac{1}{2}, z$, the distance is 3.91 A . From $N$ on the standard molecule to $F^{\prime}$, on the molecule at $\frac{1}{2}-x, \frac{1}{2}+y,-z$, the distance is 3.84 A ., to $E_{1}{ }^{\prime}$ it is 3.52 A ., and to $S_{1}{ }^{\prime} 3.74 \mathrm{~A}$. On this same pair of molecules $O$ is 3.72 A . from $E_{1}{ }^{\prime}, 3.49 \mathrm{~A}$. from $F_{1}{ }^{\prime}$, and 3.76 A . from $I_{1}{ }^{\prime}$. In the $c$-axis translation, $P$ on the standard molecule is 3.74 A . from $I_{2}$ on the molecule at $x, y, z+1$, and 4.00 A . from $J_{2}$ on the same molecule. These intermolecular distances are of about the same magnitude as is usually found in hydrocarbon structures.

## Discussion of Results.

For the reasons explained above, the accuracy of the present analysis cannot be as high as in the coronene analysis. Nevertheless, the small differences between independently estimated values for corresponding lengths in different parts of the molecule suggest that the errors are not excessive, and as described below (see p. 1407), the molecular model of Fig. 3 gives better agreement with the observed $F$ values than does a regular, hexagonal model in the same orientation. The possibility of errors amounting to $\pm 0.03 \mathrm{~A}$. for any individual bond distance cannot be excluded, but the evidence is fairly strong that the molecular co-ordinates given in Table III are, on the whole, more correct than those derived from a completely regular model. In particular, the bonds $B C$ and $H I$ are independently estimated to be $1.38 \pm 0.01 \mathrm{~A}$., and it seems very probable that these two bonds are, in fact, distinctly shorter than the other bonds observed.

A rough calculation of the bond distances can be made from the 14 non-excited valency bond structures for 1:12-benzperylene (III-XVI). By the same method as described for coronene, pyrene, and 1:2-5:6-dibenzanthracene (Robertson and White, loc. cit.) the percentage double-bond character can be calculated for each bond in the molecule, and these values are shown in (XVII).

(III.)

(X.)

(IV.)

(XI.)

(V.)

(XII.)

(VI.)

(XIII.)

(VII.)

(XIV.)

(VIII.)

(XV.)

(IX.)

(XVI.)

The corresponding bond distances obtained from Pauling and Brockway's curve ( J. Amer. Chem. Soc., 1937, 59, 1223) are given in (XVIII), and the observed distances in (XIX).


Bond orders.
(XVII.)


Distances calculated.
(XVIII.)


Distances found.
(XIX.)

There is a distinct qualitative resemblance between the observed and the calculated values, and the average value of the calculated bond distances ( 1.408 A .) is in excellent agreement with the observed average ( 1.412 A .). It should be noted that in the above calculation the 14 stable valency bond structures have been assigned equal weight, which is probably incorrect, and even more important, no account has been taken of the excited structures.

At this stage it is perhaps more noteworthy that the bond distances measured in benzperylene are very similar to those found between corresponding atoms in coronene (Robertson and White, loc. cit.). For instance, the shortest bonds in benzperylene are 1.38 A., while the corresponding bonds in coronene measure $1 \cdot 38_{5} \mathrm{~A}$. The central ring of coronene is regular with bond lengths 1.43 A ., and in benzperylene $Q R$ and $S T$ measure 1.43 A . and $R S 1.42 \mathrm{~A}$. Other bond distances in both compounds vary between the extreme values of the two groups compared above. It would appear that this pattern of variations in carbon-carbon bond distances is characteristic of this complex type of condensed-ring aromatic hydrocarbon, and in this connection it is unfortunate that in the present investigation it has not been possible to measure bond distances on the " open" side of the molecule, i.e., bonds involving the atoms $M, U, V$, and $N$, for here we should expect to find the largest differences between the coronene and the benzperylene structure. Further theoretical discussion is hardly justified until more accurate and complete measurements have been made on benzperylene or similar molecules.

## Experimental.

Determination of Crystal Data and Intensities.-The $X$-ray work was carried out photographically by means of rotation, oscillation, and moving-film methods, $\mathrm{Cu}-K_{\alpha}$ radiation being employed throughout. The axial lengths given above were checked by rotation about the diagonal of the $a b$ face and agreement was obtained to $0 \cdot 2 \%$. The density was found by flotation of small crystals in a solution of silver nitrate at $20^{\circ}$, and the highest value obtained was 1.349 in good agreement with the value of 1.338 calculated for four molecules in the unit cell.

The estimates of intensity were made visually on moving-film photographs taken about the $b$ and $c$ crystal axes. For correlation of the strongest and the weakest reflections the multiple-film technique was used (Robertson, J. Sci. Instr., 1943, 20, 175). For the main part of the work crystal specimens were employed which were small and uniform enough to make absorption error negligible. The specimen used for most of the ( $h 0 l$ ) measurements had a mean cross-section of $0.24 \mathrm{~mm} . \times 0.28 \mathrm{~mm}$. To check extinction effects, photographs were taken of small crystals which had been quenched in liquid air. The only evidence of extinction was in the strong (001) reflection, and for this reflection the highest intensity recorded was adopted as being the most probable. Considerably larger crystals were used in recording the very weakest reflections, and the final scale of intensity had the very large range of $60,000: 1$. An approximately absolute scale was obtained by correlation with the calculated $F$ values.

Fourier Analysis.-Using the measured values of F and the phase constants obtained from the trial structures, double Fourier series were set up according to the usual formulæ. The electron density was computed at 900 points on the asymmetric unit, the $a$-axis being divided into 60 parts (intervals of 0.195 A .) and the $c$-axis into 60 parts (intervals of 0.165 A .). The summations were carried out by means of three-figure strips (Robertson, Phil. Mag., 1936, 21, 176). The positions of the contour lines were obtained by graphical interpolation of the summation totals, by making sections of both the rows and columns. The contour map resulting from the final refinement is shown in Fig. 1, three-quarters of the unit cell being included.

Calculation of Molecular Orientation and Co-ordinates.-From the observed projection distances of lines parallel to $A Q$, which can be only very slightly tilted to the projection plane, it was found that the best average radius of the hexagons is $1-41 \mathrm{~A}$. The observed projection distances of $P B, A C$, and
$T G$ measure $1.286 \pm 0.025 \mathrm{~A}$. In a regular hexagonal structure of radius 1.41 A . the real distance considered would be 2.44 A . and so $\psi_{M}$, the angle between $M$ and the $b$ crystal axis, is obtained as $31.8^{\circ}$; $\psi_{L}$ cannot be derived by the same method as it is so close to $90^{\circ}$, but can be obtained indirectly from the apparent angle which $L$ makes with $M$ in projection.

The projected lines $C D G H, B R S I$, and $A \overline{1}$ make an average angle of $79 \cdot 7^{\circ} \pm 0 \cdot 2^{\circ}\left(\eta_{L}\right)$ with $a$, and the lines $P B, A C$, and $T G$ make an average angle with $a$ of $-8 \cdot 3^{\circ} \pm 0 \cdot 4^{\circ}\left(\eta_{M}\right)$. With these data and the nine trigonometrical relations given in the coronene analysis (Robertson and White, loc. cit.) the complete orientation of the molecule can be calculated with respect to the crystallographic axes $a, b$, and $c^{\prime}\left(c^{\prime}\right.$ is perpendicular to $a$ and $\left.b\right)$ and is given in Table I. The above calculation assumes that the molecule is planar and that the axes $L$ and $M$ are at right angles.

Fig. 5.


Co-ordinates assigned to the resolved atoms in the asymmetric crystal unit.
The next step is to calculate the molecular co-ordinates in terms of the axes $L$ and $M$. If we take a regular, planar model of hexagonal radius 1.41 A . and combine the molecular co-ordinates with the orientation angles of Table I, we obtain the crystal co-ordinates which this regular model would have if its centre coincided with the origin. By subtracting these co-ordinates from the $a$ and $c$ co-ordinates actually observed and averaging the eleven independent values, the free translations of the molecule along the $a$ and $c$ crystal axes are found to be 0.907 A . and 0.462 A ., respectively.

The molecular co-ordinates can now be directly calculated from the relations :

$$
\begin{gathered}
x^{\prime \prime}=x-x_{P}+z^{\prime \prime} \cot \beta \\
z^{\prime \prime}=\left(z-z_{P}\right) \sin \beta \\
L=\left(z^{\prime \prime} \cos \chi_{M}-x^{\prime \prime} \cos \omega_{M}\right) /\left(\cos \chi_{M} \cos \omega_{L}-\cos \omega_{M} \cos \chi_{L}\right) \\
M=\left(x^{\prime \prime} \cos \omega_{L}-z^{\prime \prime} \cos \chi_{L}\right) /\left(\cos \chi_{M} \cos \omega_{L}-\cos \omega_{M} \cos \chi_{L}\right)
\end{gathered}
$$

where $x_{P}=0.907 \mathrm{~A}$. and $z_{P}=0.462 \mathrm{~A}$.

The unresolved atoms were assigned co-ordinates by regularising the hexagons $R S G F E D$ and $A Q V N O P$ as far as is consistent with the observed centres of the resolved atoms in these hexagons. The final $x$ and $z$ co-ordinates of the eleven resolved atoms are plotted in Fig. 5.

Table IV.
Measured and calculated values of the structure factor.

| $h k l$. | $\begin{gathered} \sin \theta \\ (\lambda=1 \cdot 54) . \end{gathered}$ | F, meas. | F, calc. | $h k l$. | $\begin{gathered} \sin \theta \\ =1.54) . \end{gathered}$ | F, meas. | F, calc. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 001 | 0.079 | 103 | +104 | $40 \overline{1}$ | $0 \cdot 268$ | 27 | + 25 |
| 002 | $0 \cdot 158$ | 53 | - 53 | $40 \overline{2}$ | $0 \cdot 290$ | 18 | + 16 |
| 003 | $0 \cdot 237$ | 34 | + 31 | 403 | $0 \cdot 331$ | 26 | + 24 |
| 004 | $0 \cdot 316$ | 34 | - 29 | $40 \overline{4}$ | $0 \cdot 384$ | 4 | + 7 |
| 005 | $0 \cdot 395$ | 15 | - 16 | $40 \overline{5}$ | $0 \cdot 443$ | 3 | + 2 |
| 006 | $0 \cdot 473$ | 12 | - 12 | 406 | $0 \cdot 509$ | 10 | + 11 |
| 007 | $0 \cdot 552$ | 8 | $-12$ | 407 | $0 \cdot 576$ | 5 | - 4 |
| 008 | $0 \cdot 630$ | <1 | - 3 | 408 | $0 \cdot 650$ | 4 | 5 |
| 009 | $0 \cdot 709$ | 13 | + 14 | 409 | $0 \cdot 718$ | 3 | - 4 |
| 00, 10 | 0.789 | 8 | + 10 | 40, $\overline{1} 0$ | 0.796 | 3 | + 1 |
| 00, 11 | 0.866 | 6 | $-5$ | 40, II | $0 \cdot 870$ | $<1$ | 0 |
| 00, 12 | 0.945 | 2 | + 1 |  |  |  |  |
|  |  |  |  | 609 | $0 \cdot 869$ | 1 | 1 |
| 020 | $0 \cdot 130$ | 14 | $-14$ | 608 | 0.795 | $<1$ | + 2 |
| 040 | $0 \cdot 259$ | 6 | + 2 | 607 | $0 \cdot 727$ | 4 | + 5 |
| 060 | $0 \cdot 389$ | 8 | + 16 | 606 | $0 \cdot 666$ | 4 | + 7 |
| 080 | 0.519 | 14 | +15 | 605 | $0 \cdot 603$ | 11 | + 13 |
| $0,10,0$ | $0 \cdot 649$ | 8 | - 5 | 604 | 0.545 | 6 | + 7 |
| $0,12,0$ | 0.778 | 48 | + 46 | 603 | $0 \cdot 495$ | 7 | - 6 |
| 0, 14, 0 | $0 \cdot 907$ | $<7$ | + 1 | 602 | $0 \cdot 453$ | 1 | 1 |
|  |  |  |  | 601 | $0 \cdot 421$ | 6 | + 4 |
| 200 | $0 \cdot 133$ | 50 | + 50 |  |  |  |  |
| 400 | $0 \cdot 266$ | 25 | + 22 | 601 | $0 \cdot 398$ | 2 | + 3 |
| 600 | $0 \cdot 400$ | 17 | - 17 | 602 | $0 \cdot 410$ | 5 | + 6 |
| 800 | $0 \cdot 534$ | 36 | + 36 | 603 | $0 \cdot 436$ | 12 | - 11 |
| 10, 00 | $0 \cdot 665$ | 10 | - 6 | 604 | $0 \cdot 473$ | 2 | 0 |
| 12, 00 | $0 \cdot 800$ | 2 | - 2 | 605 | $0 \cdot 521$ | 2 | - 2 |
| 14, 00 | 0.931 | <1 | + 1 | $60 \overline{6}$ | $0 \cdot 574$ | 1 | + 6 |
|  |  |  |  | 607 | $0 \cdot 633$ | 2 | - 5 |
| 20, 11 | $0 \cdot 894$ | $<1$ | - 1 | 608 | 0.697 | 23 | + 21 |
| 20, 10 | $0 \cdot 819$ | 2 | $-1$ | 609 | 0.763 | 32 | + 30 |
| 209 | 0.740 | 24 | + 24 | 60, $1 \overline{0}$ | 0.830 | 2 | - 5 |
| 208 | 0.664 | 15 | + 19 | 60, II | 0.900 | 2 | 2 |
| 207 | $0 \cdot 588$ | $<1$ | - 1 |  |  |  |  |
| 206 | 0.510 | 16 | - 8 | 809 | 0.948 | 3 | 3 |
| 205 | $0 \cdot 435$ | 29 | + 23 | 808 | 0.888 | 2 | + 2 |
| 204 | $0 \cdot 360$ | 62 | + 53 | 807 | $0 \cdot 823$ | 1 | - 2 |
| 203 | $0 \cdot 290$ | 3 | + 1 | 806 | 0.766 | 1 | - 6 |
| 202 | $0 \cdot 222$ | 15 | - 14 | 805 | 0.709 | 15 | + 12 |
| 201 | $0 \cdot 165$ | 41 | - 41 | 804 | 0.659 | 1 | 0 |
|  |  |  |  | 803 | $0 \cdot 616$ | 6 | 6 |
| 201 | $0 \cdot 165$ | 83 | +83 | 802 | $0 \cdot 580$ | $<1$ | - 5 |
| $20 \overline{2}$ | $0 \cdot 193$ | 59 | - 50 | 801 | 0.562 | 10 | $+10$ |
| 203 | $0 \cdot 255$ | 19 | + 10 |  |  |  |  |
| 204 | $0 \cdot 325$ | $<1$ | - 2 | 801 | 0.524 | 10 | + 10 |
| 205 | $0 \cdot 398$ | 13 | - 21 | 802 | 0.530 | 7 | - 8 |
| 206 | $0 \cdot 471$ | 6 | + 7 | 803 | 0.549 | 3 | - 5 |
| 207 | $0 \cdot 495$ | $<1$ | $-1$ | $80 \overline{4}$ | 0.575 | 32 | + 30 |
| 208 | $0 \cdot 624$ | 2 | + 1 | 805 | 0.613 | 30 | + 30 |
| $20 \overline{9}$ | $0 \cdot 700$ | 2 | + 1 | 806 | $0 \cdot 661$ | 4 | - 4 |
| 20, $\overline{1} 0$ | $0 \cdot 779$ | $<1$ | - 1 | 807 | $0 \cdot 618$ | 1 | + 3 |
| 20, II | $0 \cdot 858$ | 1 | - 1 | 808 | 0.767 | 6 | 0 |
|  |  |  |  | $80 \overline{9}$ | 0.826 | 16 | + 14 |
| 40, 11 | 0.942 | 2 | 0 | 80, 10 | $0 \cdot 885$ | 7 | + 8 |
| 40, 10 | $0 \cdot 869$ | 2 | + 1 | 80, II | 0.950 | 4 | - 5 |
| 409 | $0 \cdot 794$ | $<1$ | + 2 |  |  |  |  |
| 408 | $0 \cdot 720$ | 5 | + 1 | 10, 08 | 0.976 | 2 | - 2 |
| 407 | $0 \cdot 647$ | 2 | - 5 | 10, 07 | 0.926 | 2 | + 3 |
| 406 | $0 \cdot 579$ | 2 | + 5 | 10, 06 | 0.872 | 6 | - 8 |
| 405 | $0 \cdot 508$ | 7 | - 7 | 10, 05 | 0.824 | 22 | + 21 |
| 404 | $0 \cdot 444$ | 1 | - 8 | 10, 04 | 0.778 | 50 | + 50 |
| 403 | $0 \cdot 383$ | 11 | + 11 | 10, 03 | $0 \cdot 729$ | 5 | + 2 |
| 402 | $0 \cdot 331$ | 9 | - 10 | 10, 02 | 0.707 | 5 | - 3 |
| 401 | $0 \cdot 290$ | 4 | - 5 | 10, 01 | $0 \cdot 682$ | 5 | + 4 |

Table IV (contd.)

| $h k l$. | $\begin{gathered} \sin \theta \\ (\lambda=1.54) . \end{gathered}$ | F, meas. | F, calc. | $h k l$. | $\begin{gathered} \stackrel{\sin \theta}{=1 \cdot 54}) . \end{gathered}$ | F, meas. | F, calc. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10, 0 I | 0.655 | 3 | + 1 | 2, 10, 0 | $0 \cdot 659$ | 28 | - 39 |
| 10, $0 \overline{2}$ | $0 \cdot 657$ | 3 | - 6 | 2, 11, 0 | 0.723 | $<9$ | - 7 |
| 10, 03 | $0 \cdot 669$ | 5 | - 9 | 2, 12, 0 | 0.778 | $<9$ | - 4 |
| 10, 04 | $0 \cdot 689$ | 4 | 0 | 2, 13, 0 | 0.855 | $<8$ | + 1 |
| 10, 05 | $0 \cdot 719$ | 20 | + 21 | 2, 14, 0 | 0.918 | $<6$ | $-2$ |
| 10, $0 \overline{6}$ | 0.753 | 4 | + 7 |  |  |  |  |
| 10, 07 | 0.795 | 2 | $-6$ |  |  |  |  |
| 10, $0 \overline{8}$ | 0.844 | 2 | + 3 | 310 | $0 \cdot 208$ | 57 | $-52$ |
| 10, 09 | 0.899 | 7 | - 5 | 320 | $0 \cdot 239$ | 64 | $+57$ |
| 10, 0, $\overline{1} \overline{0}$ | 0.954 | 6 | 4 | 330 | $0 \cdot 279$ | $<5$ | - 3 |
|  |  |  |  | 340 | $0 \cdot 327$ | <6 | + 1 |
| 12, 05 | 0.943 | $<1$ | $-1$ | 350 | $0 \cdot 380$ | $<6$ | - 3 |
| 12, 04 | $0 \cdot 900$ | 11 | + 10 | 360 | $0 \cdot 435$ | $<7$ | - 6 |
| 12, 03 | 0.868 | 14 | + 8 | 370 | $0 \cdot 495$ | $<7$ | 0 |
| 12, 02 | 0.839 | 2 | $-5$ | 380 | 0.558 | $<8$ | 0 |
| 12,01 | $0 \cdot 815$ | 2 | + 4 | 390 | $0 \cdot 614$ | 11 | - 9 |
|  |  |  |  | 3, 10, 0 | 0.678 | 16 | - 18 |
| 12, 01 | 0.789 | 10 | - 5 | 3, 11, 0 | $0 \cdot 739$ | $<9$ | - 7 |
| 12, $0 \overline{2}$ | 0.795 | $<1$ | + 2 | 3, 12, 0 | 0.803 | $<9$ | 0 |
| 12, 03 | 0.803 | 1 | $-1$ | 3, 13, 0 | 0.868 | 12 | $-4$ |
| [2, 04 | $0 \cdot 820$ | 1 | 0 | 3, 14, 0 | 0.932 | $<6$ | + 2 |
| 12, 05 | 0.833 | $<1$ | $-1$ |  |  |  |  |
| 12, 06 | $0 \cdot 871$ | $<1$ | 0 |  |  |  |  |
| 12, 07 | $0 \cdot 899$ | 1 | 1 | 410 | $0 \cdot 275$ | $<5$ | + 5 |
|  |  |  |  | 420 | $0 \cdot 293$ | <5 | + 7 |
| 14, 01 | 0.919 | 2 | + 1 | 430 | 0.330 | $<6$ | $+\quad 6$ |
| 14, $0 \underline{2}$ | 0.918 | 2 | + 2 | 440 | $0 \cdot 372$ | 8 | $-12$ |
| 14, $0 \overline{3}$ | 0.924 | $<1$ | $-1$ | 450 | $0 \cdot 419$ | $<7$ | + 4 |
|  |  |  |  | 460 | $0 \cdot 472$ | 10 | $-10$ |
| 110 | 0.093 | 66 | + 64 | 470 | 0.527 | $<8$ | - 1 |
| 120 | $0 \cdot 145$ | 49 | + 39 | 480 | $0 \cdot 580$ | $<8$ | + 7 |
| 130 | $0 \cdot 205$ | 47 | + 35 |  |  |  |  |
| 140 | $0 \cdot 268$ | 18 | - 19 |  |  |  |  |
| 150 | $0 \cdot 330$ | 5 | - 2 | 510 | $0 \cdot 341$ | 6 | + 6 |
| 160 | $0 \cdot 389$ | $<6$ | + 1 | 520 | $0 \cdot 358$ | 19 | $-21$ |
| 170 | $0 \cdot 459$ | <7 | $-12$ | 530 | $0 \cdot 387$ | 22 | $-20$ |
| 180 | 0.522 | $<8$ | + 8 | 540 | $0 \cdot 423$ | $<7$ | + 5 |
| 190 | 0.587 | $<8$ | - 1 | 550 | 0.465 | $<7$ | - 6 |
| 1, 10, 0 | $0 \cdot 651$ | 15 | $-18$ | 610 | $0 \cdot 404$ | $<6$ | + 3 |
| 1, 11,0 | 0.743 | 33 | + 24 | 620 | $0 \cdot 416$ | 24 | $-20$ |
| 1, 12, 0 | 0.781 | $<9$ | - 2 | 630 | $0 \cdot 440$ | $<7$ | + 3 |
| 1, 13, 0 | $0 \cdot 847$ | <8 | - 1 | 640 | 0.477 | $<7$ | - 6 |
| 1, 14, 0 | 0.913 | $<6$ | 0 | 710 | $0 \cdot 421$ | 12 | + 12 |
|  |  |  |  | 720 | 0.485 | $<7$ | 0 |
| 210 | $0 \cdot 147$ | 57 | + 52 | 730 | $0 \cdot 507$ | 16 | $-12$ |
| 220 | $0 \cdot 187$ | 112 | $-108$ | 740 | $0 \cdot 534$ | $<8$ | + 7 |
| 230 | $0 \cdot 236$ | 8 | +11 | 810 | 0.540 | 30 | + 28 |
| 240 | $0 \cdot 290$ | 8 | - 9 | 820 | 0.550 | 10 | +10 |
| 250 | $0 \cdot 349$ | 8 | + 6 | 830 | 0.570 | $<8$ | 0 |
| 260 | $0 \cdot 410$ | 12 | + 12 | 910 | $0 \cdot 607$ | 11 | + 14 |
| 270 | $0 \cdot 471$ | $<7$ | - 6 | 920 | $0 \cdot 617$ | $<9$ | + 3 |
| 280 | 0.535 | $<8$ | - 1 | 10, 10 | $0 \cdot 671$ | 20 | +19 |
| 290 | $0 \cdot 598$ | 18 | $-17$ | 10, 20 | $0 \cdot 681$ | <9 | - 5 |

The co-ordinates of Table II ( $a$ ) were used for a final calculation of the structure factors of the ( $h 0 l$ ) and ( $h k 0$ ) reflections and the results are collected in Table IV under " $\mathrm{F}_{2}$ calc." It was found that on the basis of the usual hydrocarbon scattering curve (Robertson, Proc. Roy. Soc., 1935, A, 150, 110) the calculated structure factors for small-spacing planes were consistently higher than the observed values and the empirical scattering curve adopted for high $\sin \theta$ values is given below (max. $\mathrm{f}_{\sigma}=100$ ).

For the ( $h 0 l$ ) zone, the mean discrepancy, expressed as

$$
\frac{\Sigma(\mid F, \text { meas. }|-| F, \text { calc. } \mid)}{\Sigma \mid F, \text { meas. } \mid}
$$

was found to be $16.6 \%$, for the $h k 0$ zone $10.9 \%$, and for all the reflections together, $14 \cdot 1 \%$.
If instead of the co-ordinates of Table II, co-ordinates derived from a regular, hexagonal model in the orientation of Table I are employed for calculation of the ( $h 0 l$ ) structure factors, the mean discrepancy increases to $18.5 \%$, indicating that the given co-ordinates are preferable.

The author wishes to thank Professor J. Monteath Robertson, F.R.S., for his continued interest in this problem and for helpful discussion, Professor J. W. Cook, F.R.S., for some beautiful crystal specimens of 1:12-benzperylene and perylene, and the Carnegie Trustees for a scholarship held during the earlier part of this work.

The University, Glasgow. [Received, September 5th, 1947.]

